

Bitcoin Transactions

Goal: enable digital payments between untrusted parties
with no central authority (no companies, governments, etc).

Ingredients of a Bitcoin transaction:

- ① Sender } specified by "public key"
- ② receiver
- ③ amount to transfer (in BTC)
[currently 1BTC ≈ 10K USD]
- ④ pointer to last transaction with these coins
- ⑤ transaction fee

Valid transaction:

- cryptographically signed by sender
- sender = owner of coins

P2P Network: used to broadcast all transactions to everybody.

The Blockchain

Ledger: history of all transactions authorized thus far. (grouped into "blocks")

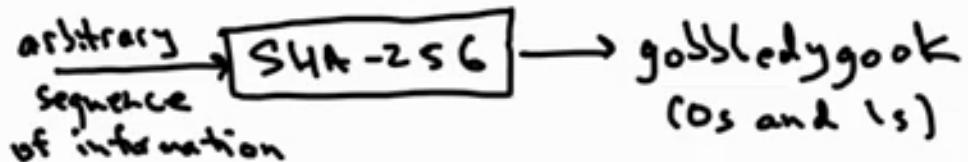
Ingredients of a block: ① some transactions (typically 1000 - 2000)
② reference to preceding block ③ a "nonce"



Key idea: ① incentivize "miners" to add blocks (+ collect reward in BTC) BUT
② make it hard to do so ("proof of work")
how BTCs get "minted"!

Mining

Cryptographic hash function:



[In practice, SHA-256 indistinguishable from a random function]

Call a block b eligible if $\text{SHA-256}(b)$ starts with 80 zeroes.

Bitcoin mining: ① try to find eligible block b ② broadcast it across P2P network

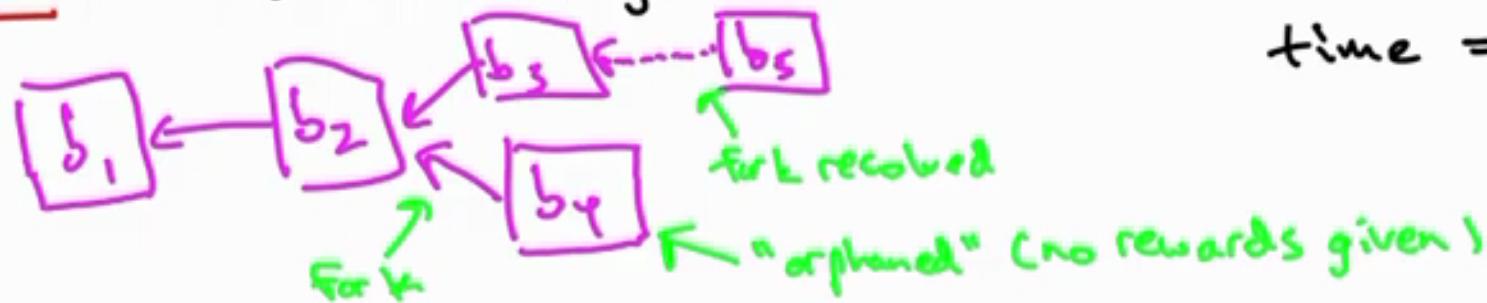
Reward: 6.25 BTC (+ transaction fees) ⇒ gets appended to Blockchain

Belief: no algorithm better than random guessing. ⇒ on average, succeed every 2^{80} tries

Why 80?: want new block added every 10 minutes on average.

Forks

Issue: two different eligible blocks discovered at roughly the same time \Rightarrow fork.



Specified behavior: interpret authorized transactions as those in the longest chain (break ties in favor of block you heard about it first).

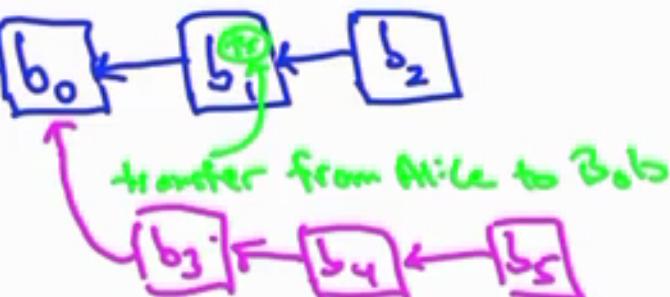
Consequence: regard a transfer of funds as complete only after transaction added to block chain **and** extended by several more blocks (e.g., 6).

Forking Attacks

Good news: Sybil attacks (i.e., create multiple IDs) ineffective.

Double-spend attack:

- Alice pays Bob in block b_1
- block b_2 added after b_1
- Alice tries to extend b_0 3 times before anyone extends b_2 (^{=1 would orphan b_1, b_2})



51% Attack: if $\alpha > \frac{1}{2}$, winner can act like a centralized authority.

- e.g., can freeze assets of any user

if Bob waits for k blocks to be added, drops to α^{k+2}

success probability = α^3
[α = fraction of overall computational power possessed by Alice]

Selfish Mining

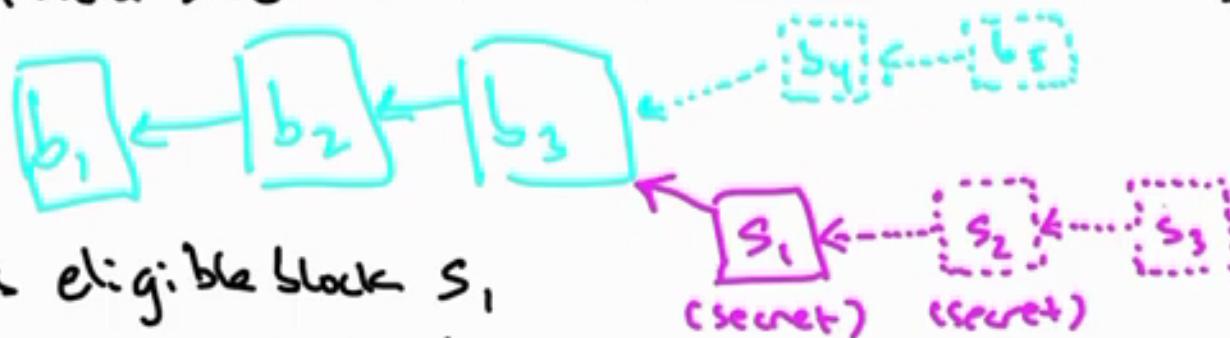
(Eyal/Gün Sitter 2014)

Second genre & attack: block withholding.

(don't tell other miners
about your eligible block)

Intuition: withhold block \Rightarrow trick other miners into working on wrong
cryptopuzzle.

Strategy:



- Alice finds eligible block s_1
- privately try to extend s_1 with another block s_2
- if by (extending b_3) announced first, Alice restarts
- if s_2 found first:
 - ① Alice mines secret chain until "lead" drops to 1
 - ② announce entire secret chain

Theorem:

Selfish mining
better than
honest mining
when $\alpha > 1/3$.

Fraction of overall computational power controlled by miner
Tim Roughgarden (Columbia University)